

Section 1: Multiple Choice (4 points each, 40 points total)

1. Which of the following best describes the purpose of using factors of safety in mechanical design?
 - ☐ To optimize material usage
 - ☐ To ensure that a design can withstand more load than expected
 - ☐ To reduce production costs
 - ☐ To minimize the weight of the design
2. Which of the following best describes the Maximum Normal Stress (MNS) theory?
 - ☐ Failure occurs when the maximum shear stress exceeds a critical value.
 - ☐ Failure occurs when the maximum normal stress exceeds the ultimate tensile strength.
 - ☐ Failure occurs when the strain energy density exceeds the failure threshold.
 - ☐ Failure occurs when the von Mises stress exceeds the yield strength.
3. Which failure criterion is typically used for ductile materials in static loading?
 - ☐ Modified Mohr theory
 - ☐ Distortion Energy Theory
 - ☐ Maximum Principal Stress Theory
 - ☐ Brittle Coulomb-Mohr theory
4. When analyzing a beam subjected to torsion, which of the following stresses must be evaluated?
 - ☐ Normal stress
 - ☐ Shear stress
 - ☐ Bending stress
 - ☐ Hoop stress
5. Which of the following best describes the purpose of conceptual design?
 - ☐ To generate detailed design drawings
 - ☐ To develop initial ideas and possible solutions
 - ☐ To select final materials
 - ☐ To test prototypes
6. The critical stress intensity factor, K_{IC} , is also known as the:
 - ☐ Tensile strength
 - ☐ Fracture energy
 - ☐ Fracture toughness
 - ☐ Geometry
7. Which of the following is NOT an assumption of static failure analysis?
 - ☐ Material exhibits linear elastic behavior up to failure.
 - ☐ Stresses are time dependent.
 - ☐ The loading is applied gradually and remains constant.
 - ☐ Failure is governed by a single, instantaneous load event.

8. What does the slope of the linear portion of a stress-strain curve represent for a material?
 - ☐ Yield strength
 - ☐ Modulus of elasticity (Young's modulus)
 - ☐ Ultimate tensile strength
 - ☐ Toughness
9. Which of the following failure criteria is most appropriate for analyzing the failure of a ductile material under static loading?
 - ☐ Modified Mohr (MM) theory
 - ☐ Maximum Shear Stress (MSS) Theory
 - ☐ Maximum Normal Stress (MNS) Theory
 - ☐ Brittle Coulomb-Mohr (BCM) theory
10. In a beam subject to pure bending, which type of stress is experienced along the length of the beam?
 - ☐ Shear stress
 - ☐ Normal stress
 - ☐ Torsional stress
 - ☐ Hoop stress

Section 2: Problem-Solving (60 points total)

11. (20 points) A circular shaft with a diameter of 30 mm is subjected to a bending moment of 600 N·m and a torsional moment of 200 N·m. The shaft is made of a brittle material with an ultimate strength in tension of 100 MPa, and an ultimate strength in compression of 400 MPa. Using the Modified-Mohr theory, determine whether the shaft will fail. Show all calculations.

12. (40 points total) Rod OAB has length $3L$ and diameter $d = L/6$.

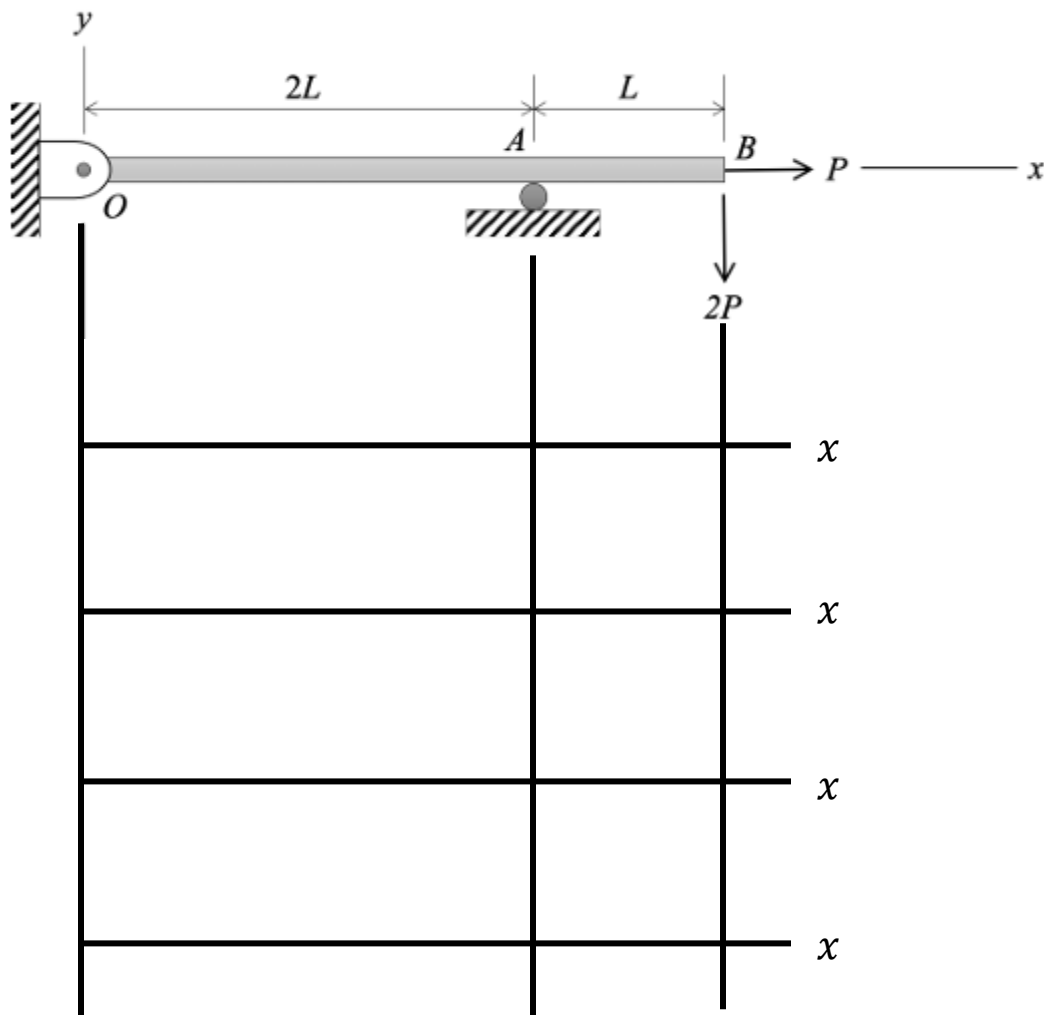
The rod is supported by a pin joint at O and by a roller at A .

Axial load P and transverse load $2P$ act at B .

The rod is made of a ductile material with yield strength S_y .

Determine the following:

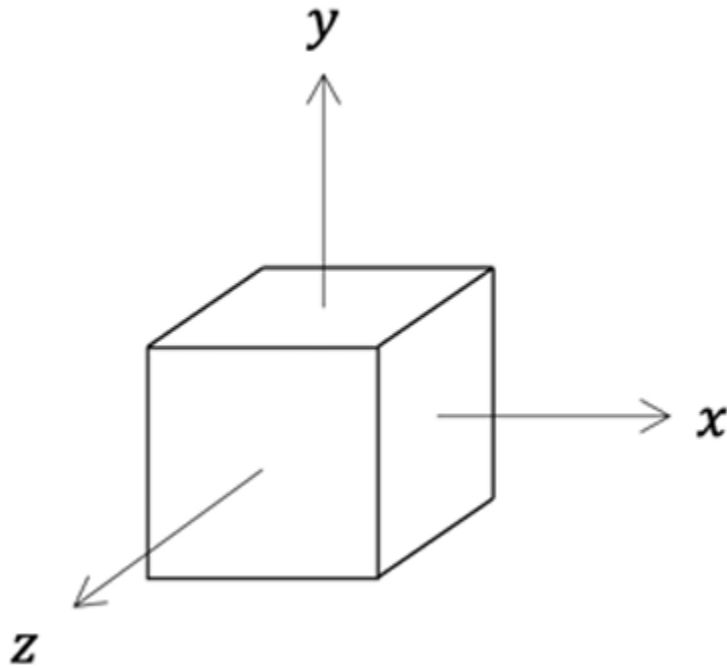
- (5 points) Solve for the reactions at O and A .
- (10 points) Sketch and label diagrams of the internal loads on the axes provided.
- (5 points) Identify the critical cross-section of rod OAB .
- (5 points) Identify the critical element on the cross-section identified in part (c).
You may use the attached Combined Stress Analysis Worksheet to aid your analysis.
- (5 points) Show the state of stress on a stress element for the critical element.
- (10 points) The factor of safety for the critical element in terms of variables P , L , and S_y . Use both the distortion energy (DE) and maximum shear stress (MSS) failure theories. If needed, axes to draw Mohr's circle are provided on the next page.



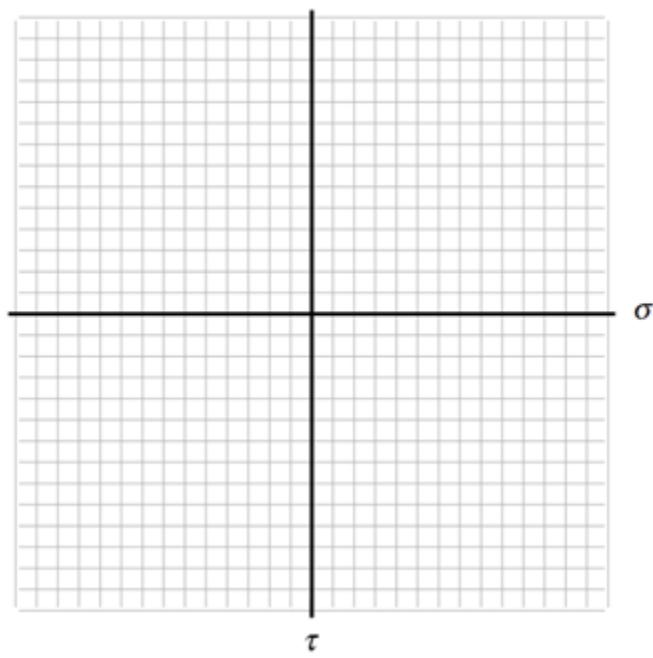
[Problem 12 continued]

[Problem 12 continued]

Stress element for the critical element:



Axes to draw Mohr's circle:



<div>In this box,<ul style="list-style-type: none">• Draw the critical cross-section• Identify and label the potential locations for the critical element(s) (e.g. top, bottom, left, right, and center)</div>					
Internal load	Potential location of critical element				
	Axial				
	Torsion				
	Transverse shear				
Stress element					
Bending		